



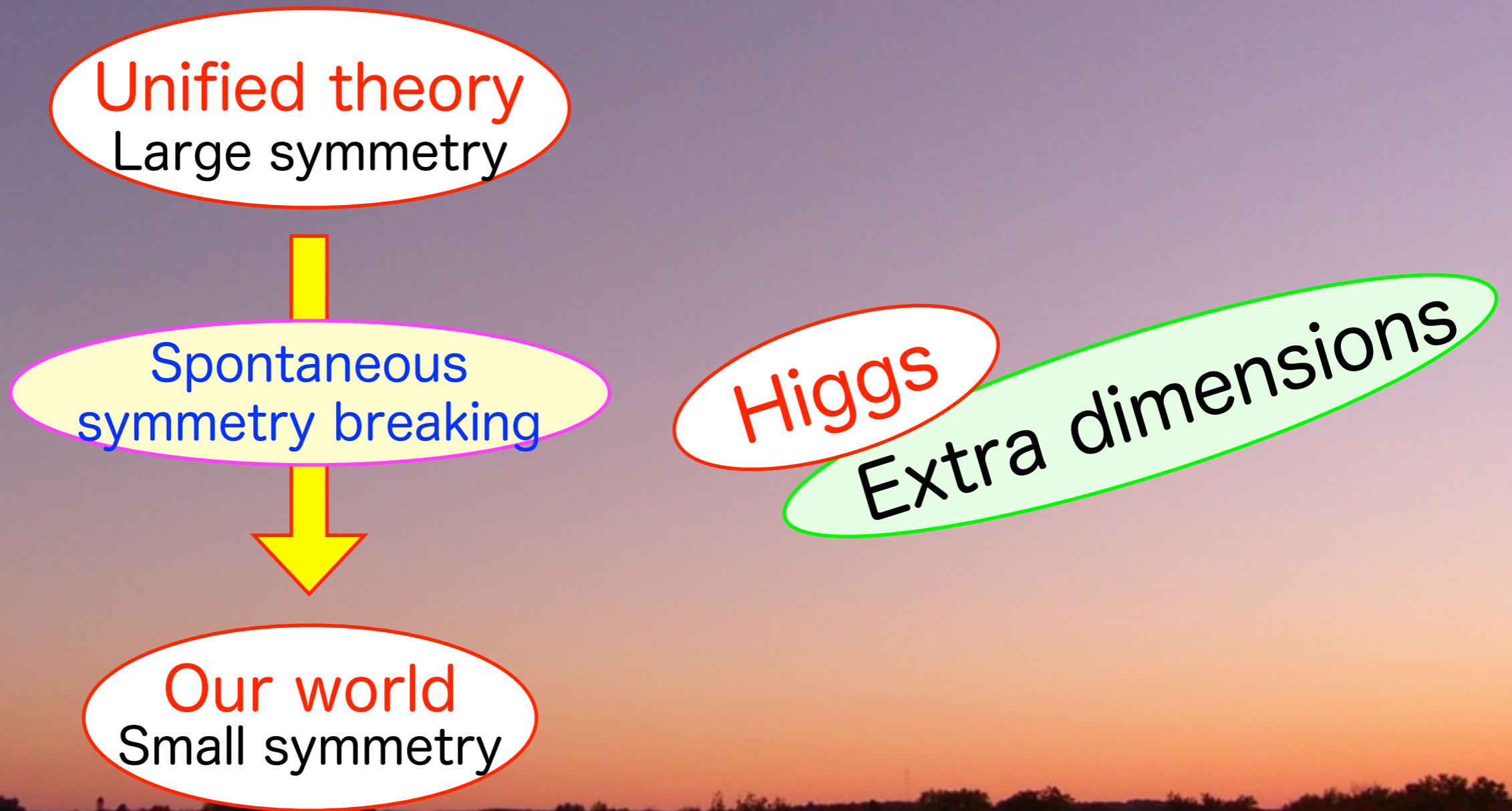
# 余剰次元における ゲージ・ヒッグス統合と LHCでのシグナル

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ICEPP (Univ of Tokyo), 14 April 2011

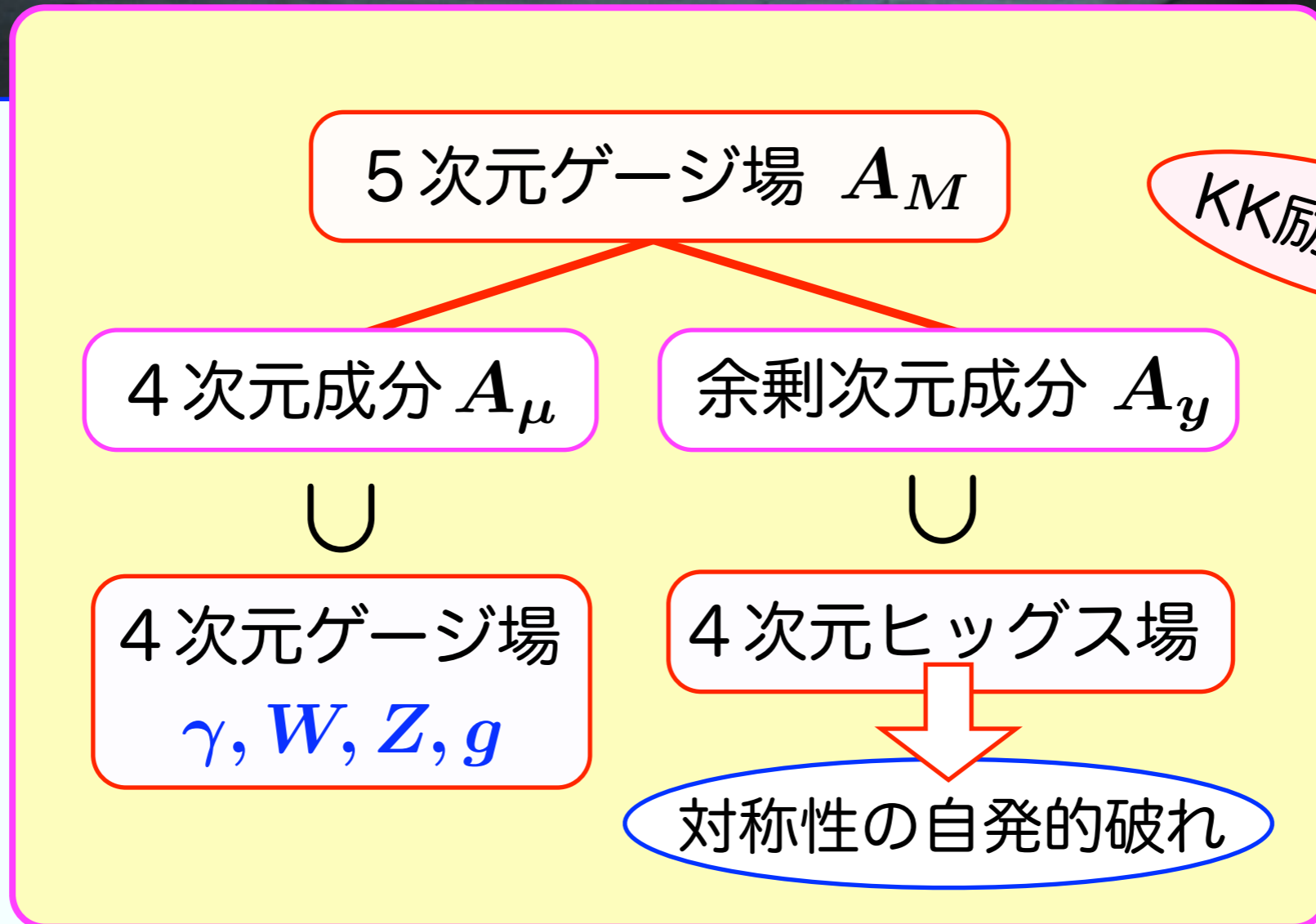
Hosotani, Tanaka, Uekusa, 1103.6076

# 力の統一



# ゲージ・ヒッグス統合理論

Hosotani 1983, 1989  
Davies, McLachlan 1988, 1989  
Hatanaka, Inami, Lim, 1998



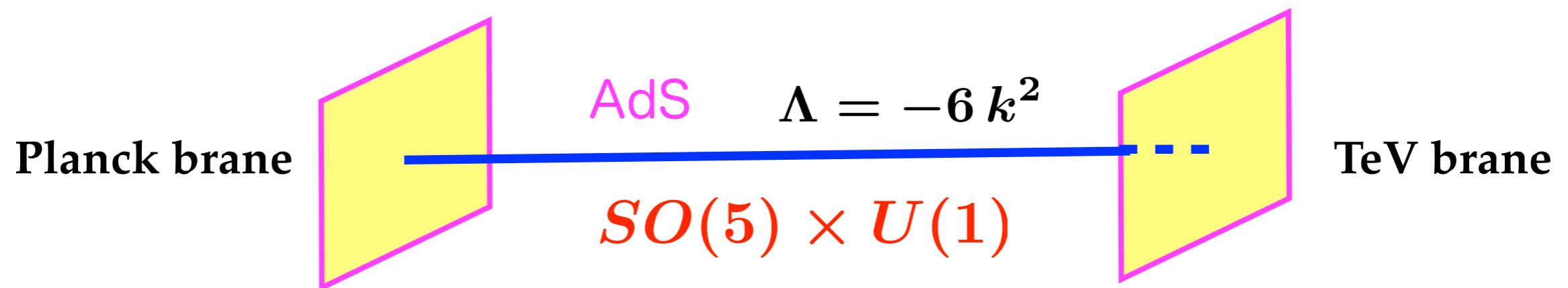
LHCでどのように見るか

# $SO(5) \times U(1)$ in Randall-Sundrum warped space

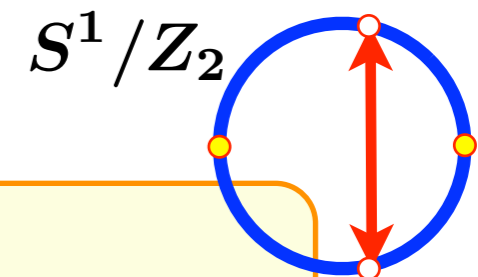
$$ds^2 = e^{-2k|y|} dx_\mu dx^\mu + dy^2$$

$$0 \leq |y| \leq L = \pi R$$

Agashe, Contino, Pomarol 2005  
 Hosotani, Sakamura 2006  
 Medina, Shah, Wagner 2007



*Orbifold BC*



$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, -y) = P_0 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, y) P_0^\dagger$$

$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, \pi R - y) = P_1 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, \pi R + y) P_1^\dagger$$

# 4D gauge bosons and Higgs

$$P_0 = P_1 = \begin{pmatrix} -1 & & & & \\ & -1 & & & \\ & & -1 & & \\ & & & -1 & \\ & & & & +1 \end{pmatrix}$$



*W Z γ*

$A_\mu \sim$



$$SO(5) \rightarrow SO(4) \simeq SU(2)_L \times SU(2)_R$$



*Higgs*

$A_y \sim$

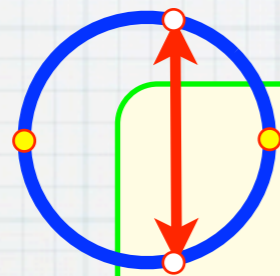
$$\begin{pmatrix} \begin{matrix} \phi_1 \\ \phi_2 \\ \phi_3 \\ \phi_4 \end{matrix} \\ \square \end{pmatrix}$$

$$\Phi = \begin{bmatrix} \phi_1 + i\phi_2 \\ \phi_4 - i\phi_3 \end{bmatrix}$$

4D Higgs doublet

# Matter content

## Chiral fermions on orbifolds



$$\Psi(x, -y) = \gamma^5 P_0 \Psi(x, y)$$

$$\Psi(x, \pi R - y) = \gamma^5 P_1 \Psi(x, \pi R + y)$$

$$\begin{pmatrix} T_L \\ B_L \\ t_L \\ b_L \\ t'_R \end{pmatrix}_{\frac{2}{3}}$$

zero (light) modes

# Matter content

YH, Noda, Uekusa 2009

(YH, Oda, Ohnuma, Sakamura 2008)

Planck brane

$SO(5) \times U(1)$

TeV brane

Quarks

$$\begin{pmatrix} \hat{T}_R \\ \hat{B}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{U}_R \\ \hat{D}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{X}_R \\ \hat{Y}_R \end{pmatrix}$$

$$\begin{pmatrix} T_L \\ B_L \\ t_L \\ b_L \\ t'_R \end{pmatrix}_{\frac{2}{3}}$$

$$\begin{pmatrix} U_L \\ D_L \\ X_L \\ Y_L \\ b'_R \end{pmatrix}_{-\frac{1}{3}}$$

$$\Psi(x, -y) = P_0 \gamma^5 \Psi(x, y)$$

Brane scalar

$$\hat{\Phi} \left(0, \frac{1}{2}\right)$$

$$\langle \hat{\Phi} \rangle \neq 0$$

$$\left(\frac{1}{2}, 0\right)$$

vector rep

$$\left(\frac{1}{2}, \frac{1}{2}\right) \oplus (0, 0)$$

$$\begin{pmatrix} \hat{L}_{2XR} \\ \hat{L}_{2YR} \end{pmatrix}$$

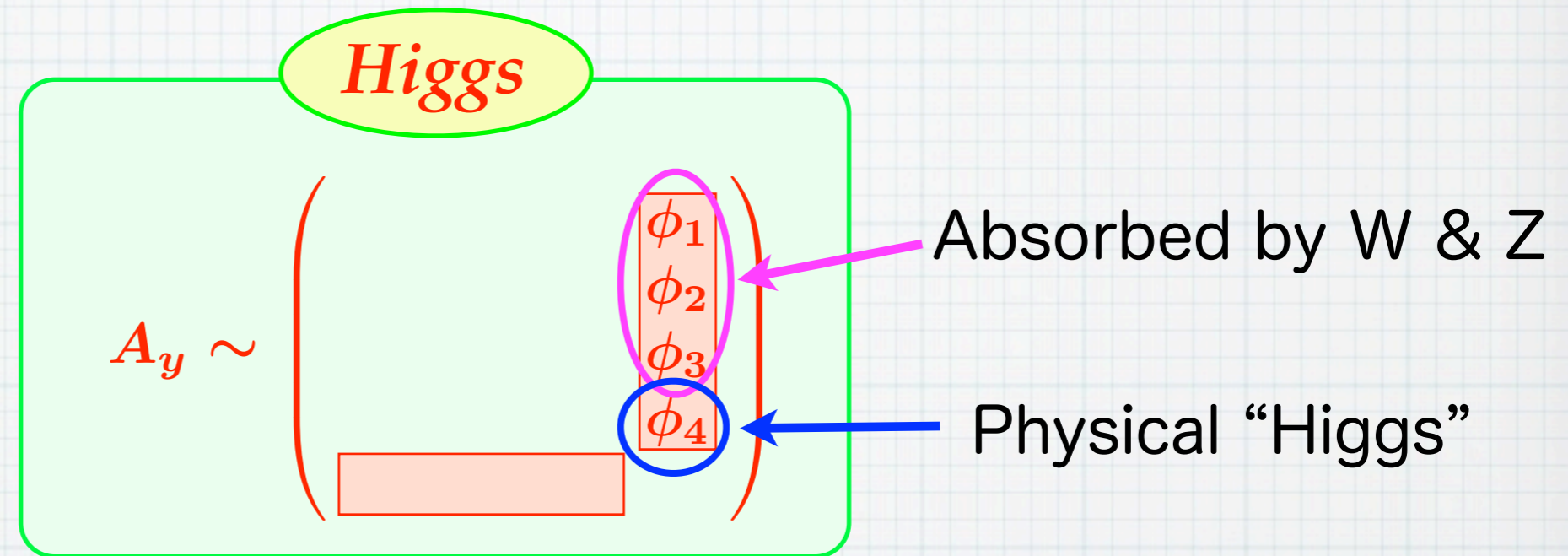
$$\begin{pmatrix} \hat{L}_{3XR} \\ \hat{L}_{3YR} \end{pmatrix}$$

$$\begin{pmatrix} \hat{L}_{1XR} \\ \hat{L}_{1YR} \end{pmatrix}$$

$$\begin{pmatrix} \nu_{\tau L} \\ \tau_L \\ L_{1XL} \\ L_{1YL} \\ \tau'_R \end{pmatrix}_{-1}$$

$$\begin{pmatrix} L_{2XL} \\ L_{2YL} \\ L_{3XL} \\ L_{3YL} \\ \nu'_{\tau R} \end{pmatrix}_0$$

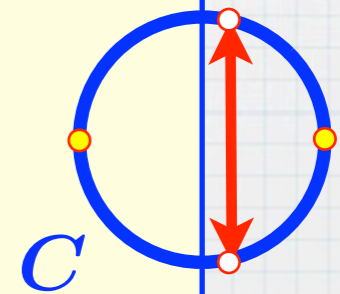
Leptons



Higgs boson as an AB phase in extra dim

$$e^{i\hat{\theta}_H(x)} \sim P \exp \left\{ ig \int_C dy A_y \right\}$$

$$\hat{\theta}_H(x) = \theta_H + \frac{H(x)}{f_H}$$





## Effective interactions

$$\text{AB phase} \quad \hat{\theta}_H = \theta_H + \frac{H}{f_H} \quad f_H = \frac{2}{\sqrt{kL}} \frac{m_{KK}}{\pi g}$$

$$\mathcal{L}_{\text{eff}} \sim -V_{\text{eff}}(\hat{\theta}_H)$$

YH 1983, Oda-Weiler 2005

Falkowski 2007

$$-m_W (\hat{\theta}_H)^2 W_\mu^\dagger W^\mu - \frac{1}{2} m_Z (\hat{\theta}_H)^2 Z_\mu Z^\mu$$

Sakamura-YH 2006, 2007

$$-m_f (\hat{\theta}_H) \bar{\psi}_f \psi_f$$

YH-Kobayashi 2008

$$\theta_H \sim \theta_H + 2\pi$$

## Gauge-Higgs

$$m_W(\hat{\theta}_H) \sim \frac{1}{2} g \underline{f_H \sin \hat{\theta}_H}$$

$$m_Z(\hat{\theta}_H) \sim \frac{1}{2 \cos \theta_W} \underline{g f_H \sin \hat{\theta}_H}$$

$$m_f(\hat{\theta}_H) \sim y_f \underline{f_H \sin \hat{\theta}_H}$$

$$\hat{\theta}_H = \theta_H + \frac{H}{f_H}$$

*periodic  
nonlinear*

## SM

$$\frac{1}{2} g \underline{(v + H)}$$

$$\frac{1}{2 \cos \theta_W} g \underline{(v + H)}$$

$$y_f \underline{(v + H)}$$



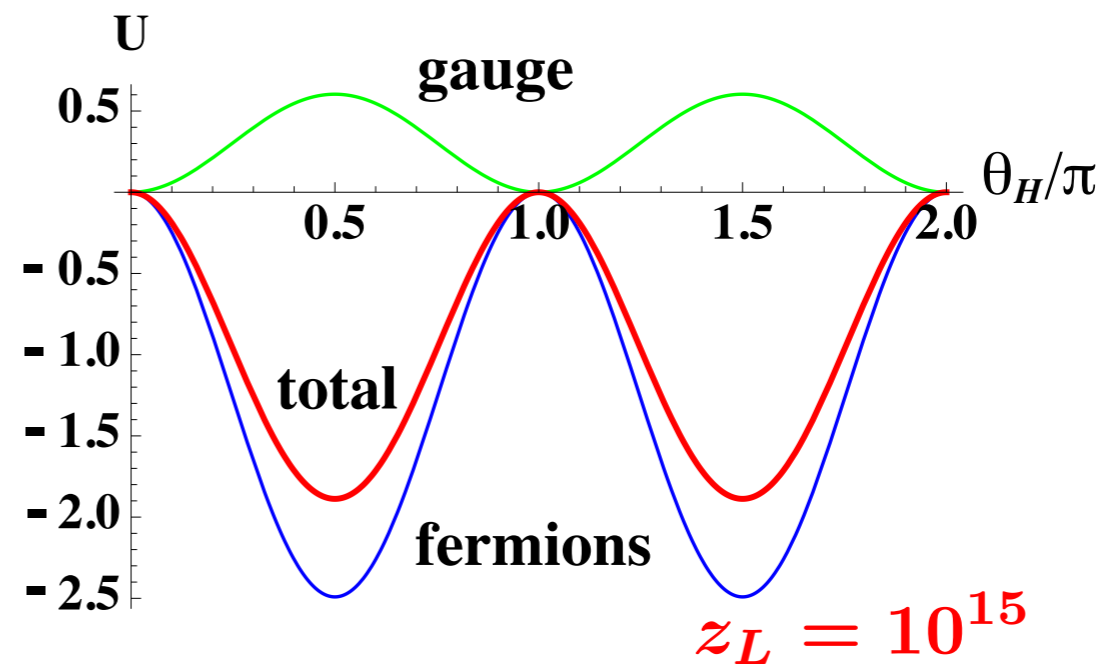
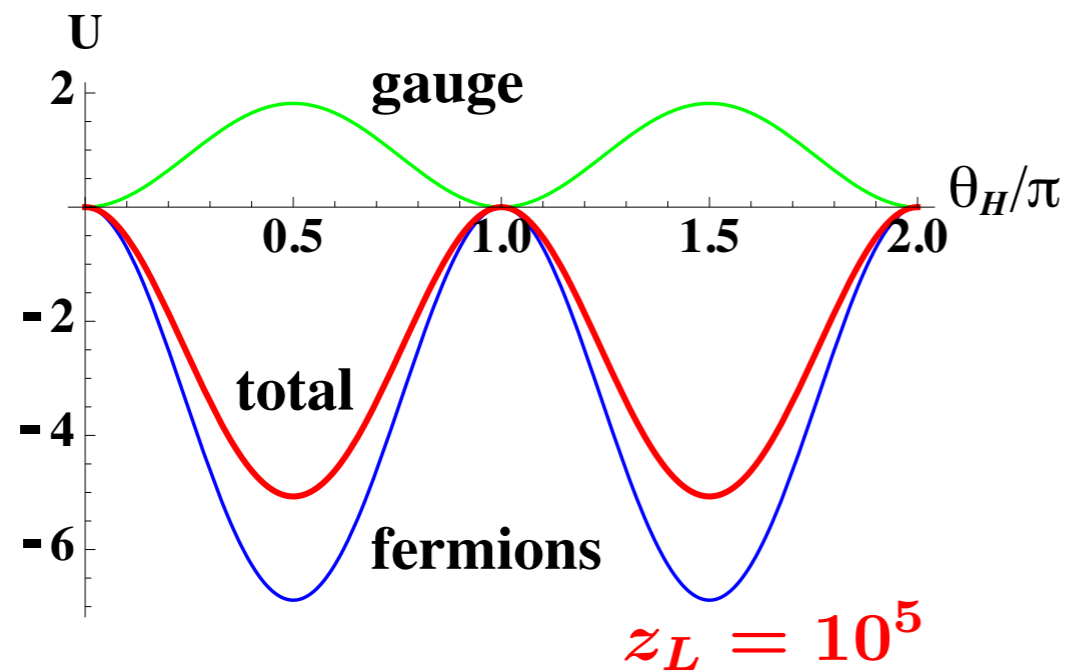
WWH  
ZZH  
Yukawa

$$= SM \times \cos \theta_H$$

WWHH  
ZZHH

$$= SM \times \cos 2\theta_H$$

# Energy density / $m_{\text{KK}}^4$



$$\theta_H = \frac{\pi}{2}$$



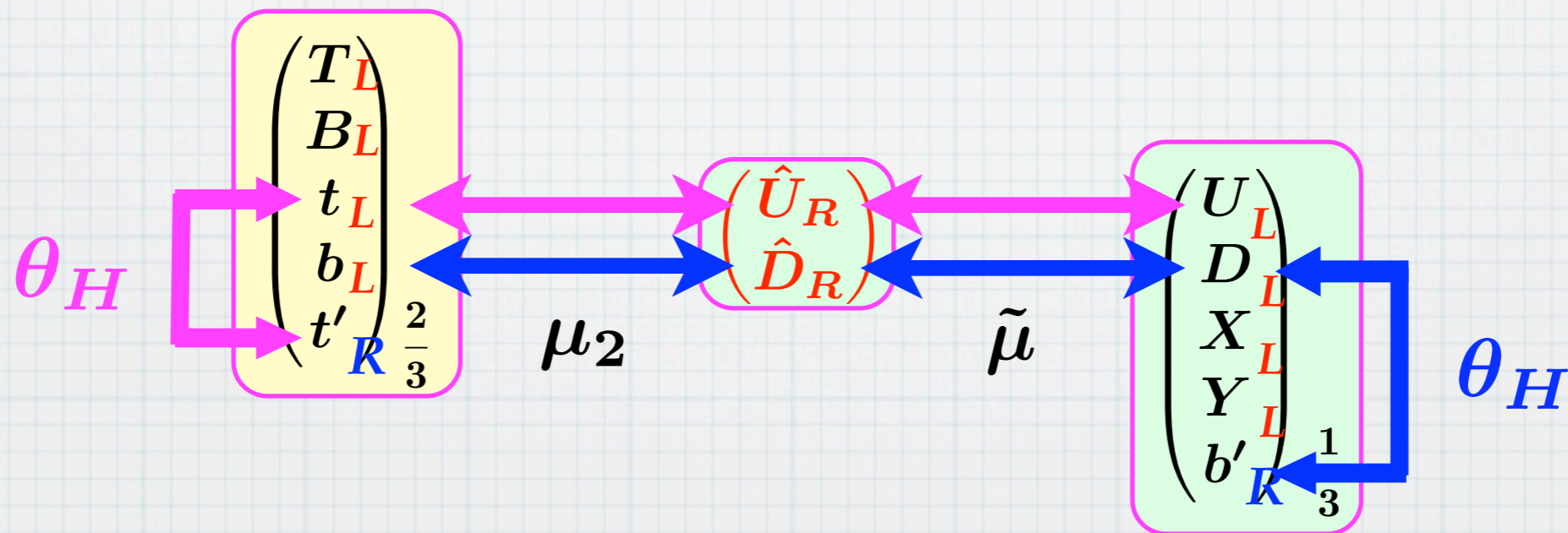
EW symmetry breaking by Hosotani mechanism

$$WWH, ZZH, \text{Yukawa} = 0$$

# Masses & Yukawa couplings

$$g_A \bar{\Psi} A_\mu \gamma^5 \Psi \quad \theta_H + \frac{H}{f_H}$$

$\Psi_L, \Psi_R$  couple by gauge int.



$$m(\hat{\theta}_H)\bar{\psi}\psi$$

$$= m(\theta_H)\bar{\psi}\psi + m^{(1)}(\theta_H)\frac{H}{f_H}\bar{\psi}\psi + \frac{1}{2}m^{(2)}(\theta_H)\frac{H^2}{f_H^2}\bar{\psi}\psi + \dots$$

Yukawa

$$\sim m_f\bar{\psi}\psi + 0 - \frac{m_f}{2f_H^2}H^2\bar{\psi}\psi + \dots$$

# H parity $H \rightarrow -H$

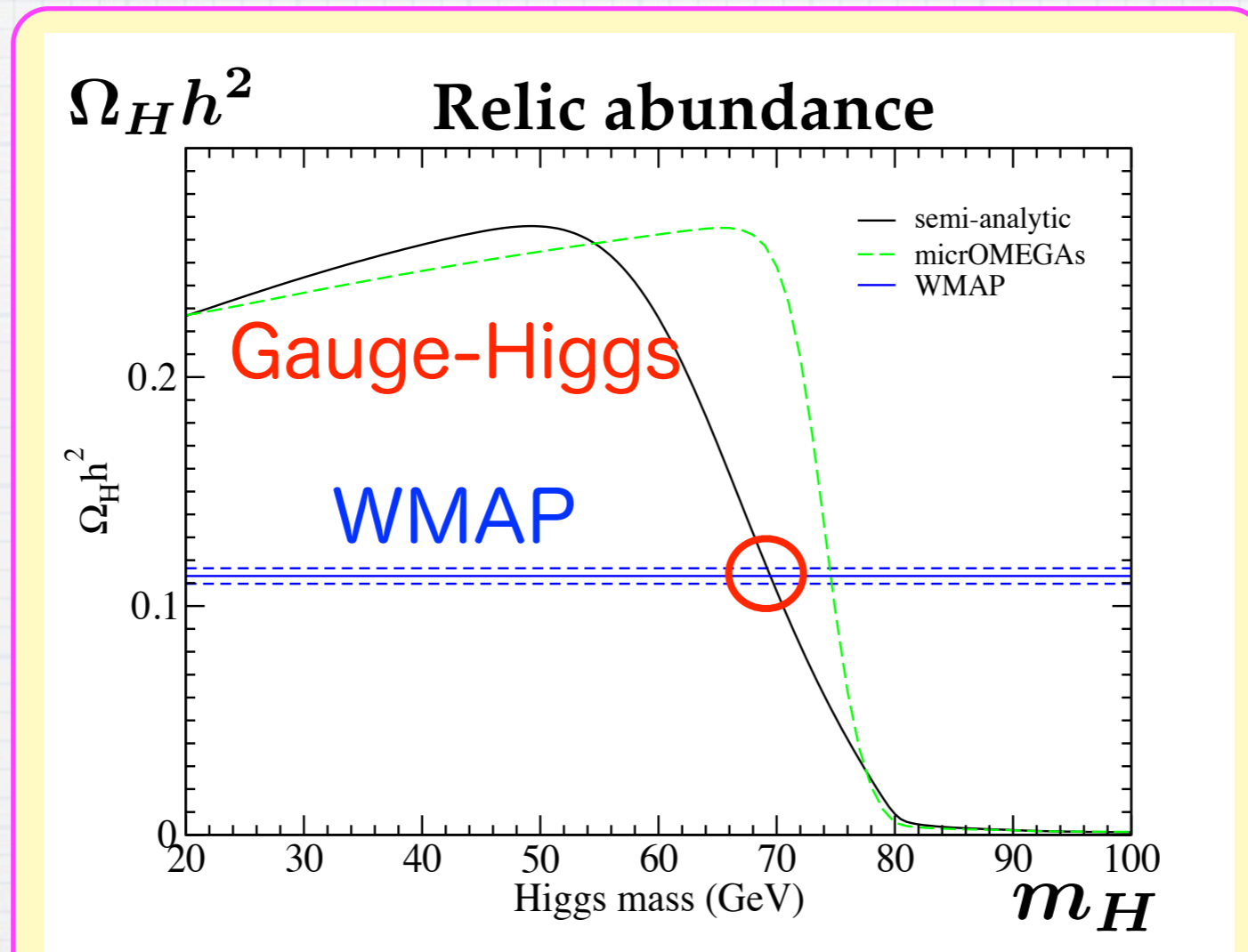
$$P_H = \begin{cases} + & W^{(n)}, Z^{(n)}, \gamma^{(n)}, gluon^{(n)}, q^{(n)}, \ell^{(n)}, \dots \\ - & H^{(n)}, W'^{(n)}, Z'^{(n)}, q'^{(n)}, \ell'^{(n)}, \dots \end{cases}$$

Higgs field : the lightest  $P_H$ -odd field.

$WWH, ZZH, Yukawa = 0$

Stable

# Stable Higgs → Dark Matter

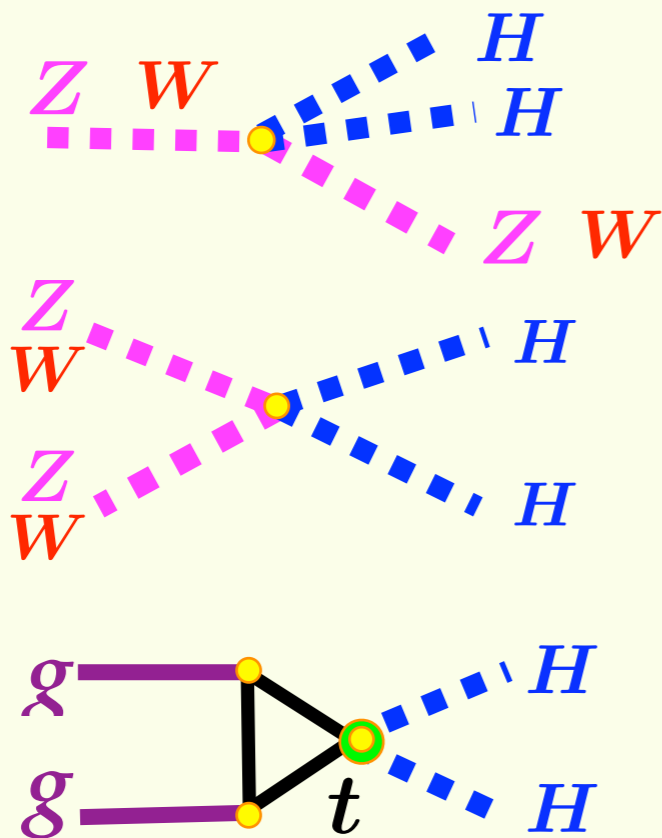


WMAP data →  $m_H \sim 70$  GeV

$z_L$	$10^5$	$10^{10}$	$10^{15}$
$m_H$	72 GeV	108	135

# How to see the Higgs bosons at LHC/ILC

## Production:



Stable Higgs boson

=

missing energy,  
missing momentum

Cheung, Song, 1004.2783

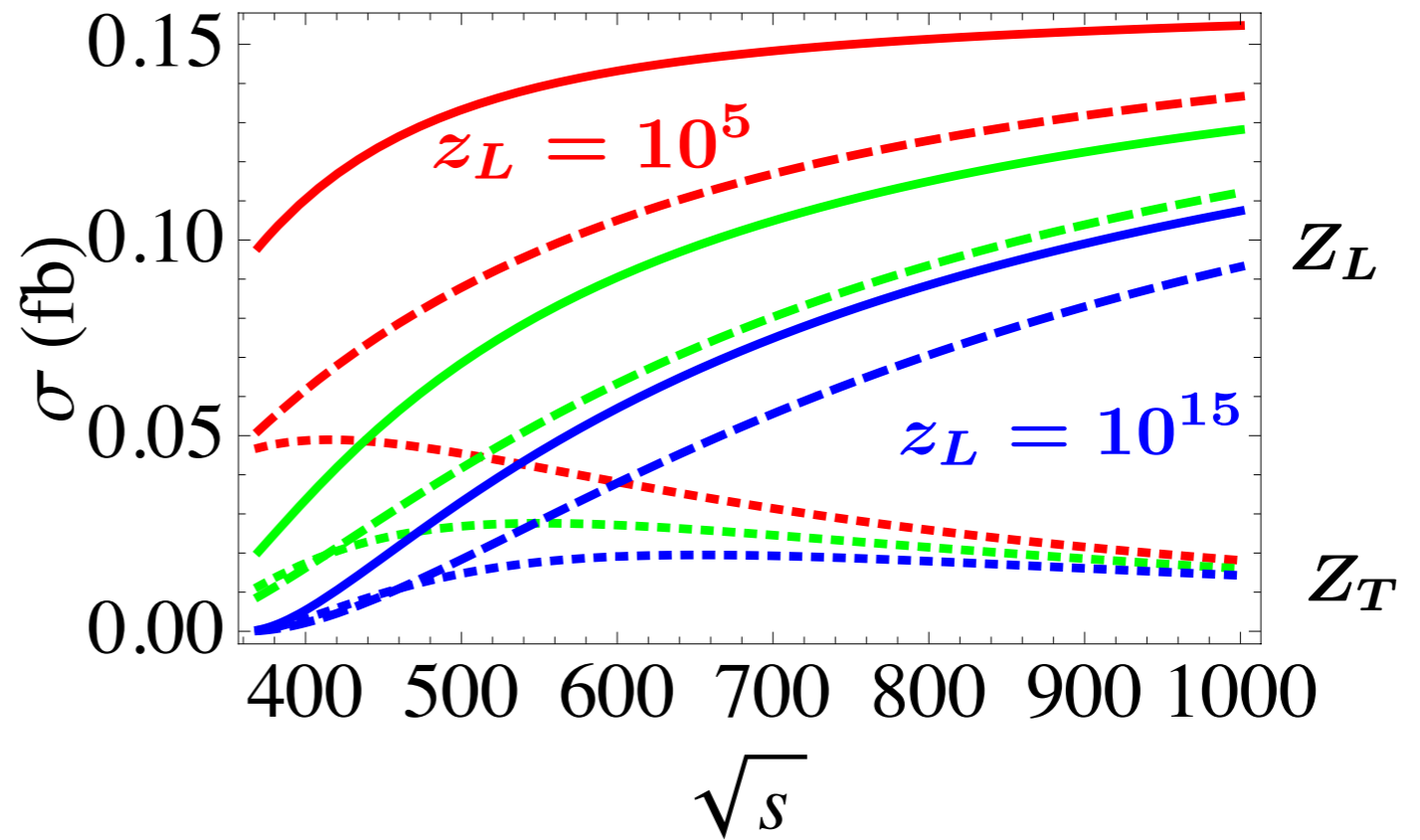
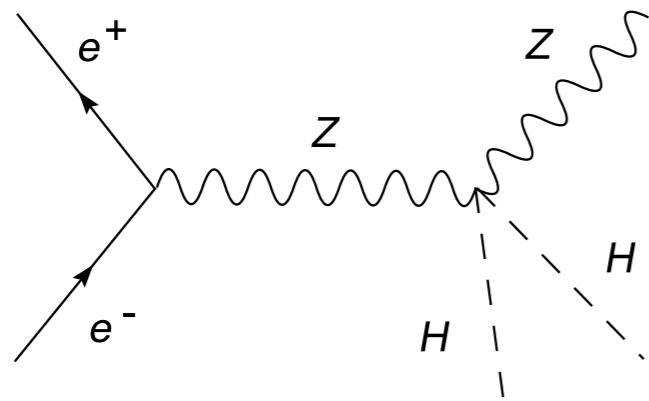
Alves, 1008.0016

$\nu, \bar{\nu}$  background

hard at LHC, possible at ILC



$$e^+e^- \rightarrow ZHH$$



major background  $e^+e^- \rightarrow Z\nu\bar{\nu}$

Polarized  $e^\pm$

$\sqrt{s} = 750 \text{ GeV}$ ,  $z_L = 10^{15}$ ,  $M_{\text{mis}} > 250 \text{ GeV}$ ,  $|\cos \theta| < 0.6$

**$L > 2.0 \text{ ab}^{-1}$  for  $5\sigma$**

## Gauge couplings precision measurements

Forward-backward asymmetry in  $e^+e^- \rightarrow Z \rightarrow \ell\bar{\ell}, q\bar{q}$

Z-decay widths (branching fractions)

	No. data	SM	$z_L : 10^{15}$	$z_L : 10^{10}$	$z_L : 10^5$
$\sin^2 \theta_W$		0.2312	0.2309	0.2303	0.2284
$\chi^2(AFB)$	6	10.8	6.3	6.4	7.1
$\chi^2(Z \text{ decay})$	8	13.6	16.5	37.7	184.5

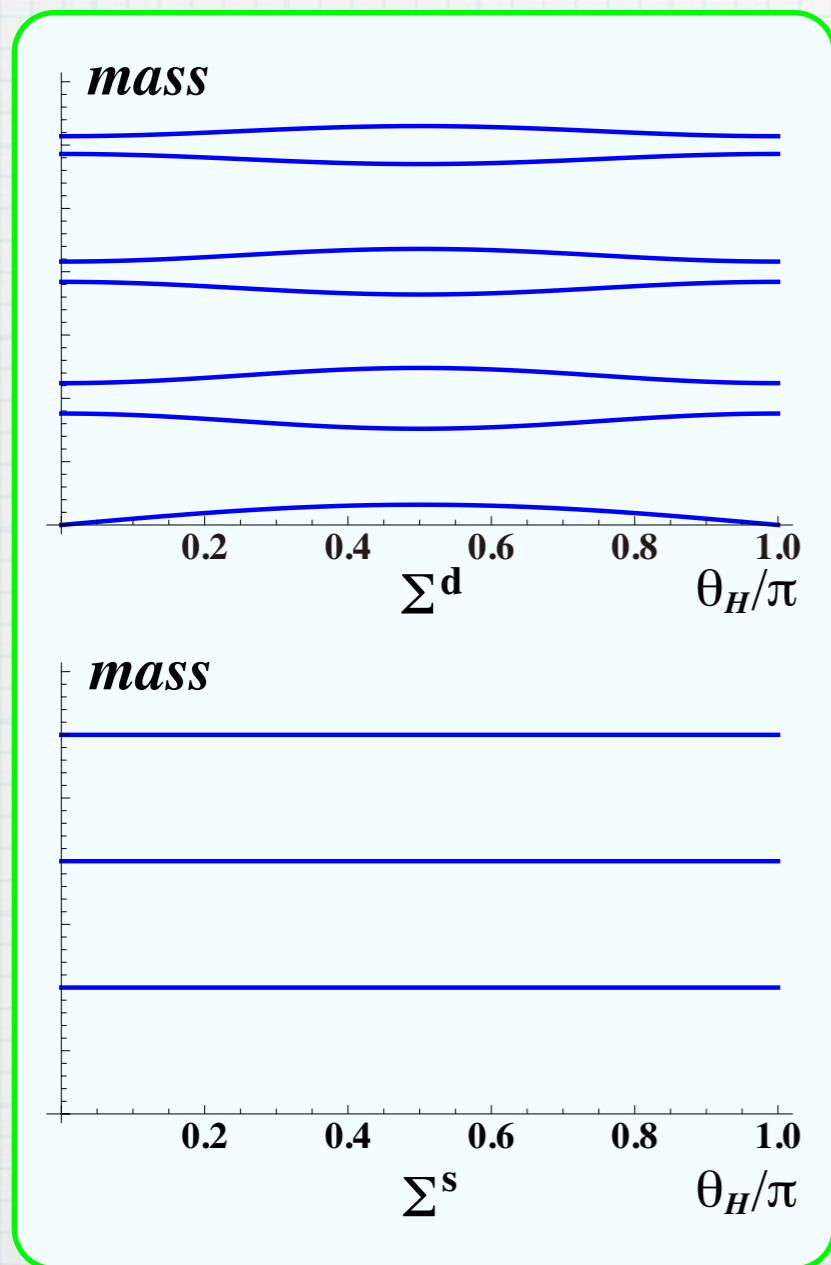

 $z_L \geq 10^{15}$

**Observe extra dimension**



**KK modes**

# 1st KK modes



	$z_L : 10^{15}$	$z_L : 10^5$
$m_{\text{KK}}$	1466	836
$Z^{(1)}$	1130	653
$gluon^{(1)}$	1144	678
$u^{(1)}$	1361	1037
$t^{(1)}$	1121	634
	in GeV	

# KK $Z^{(1)}$

$z_L$	$10^5$	$10^{15}$
$m$	653	1130
$\Gamma$	101	415

in GeV

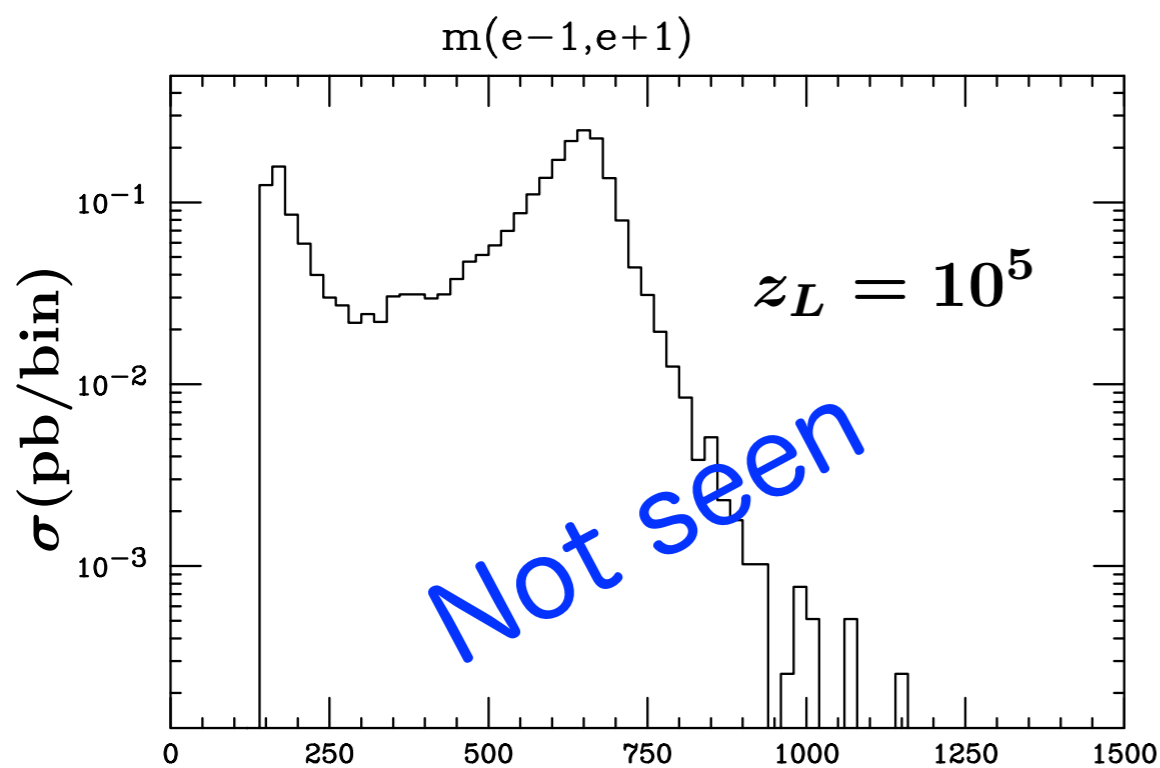
Large couplings for **right**-handed quarks and lepton

$\sim \times 10$

Large width

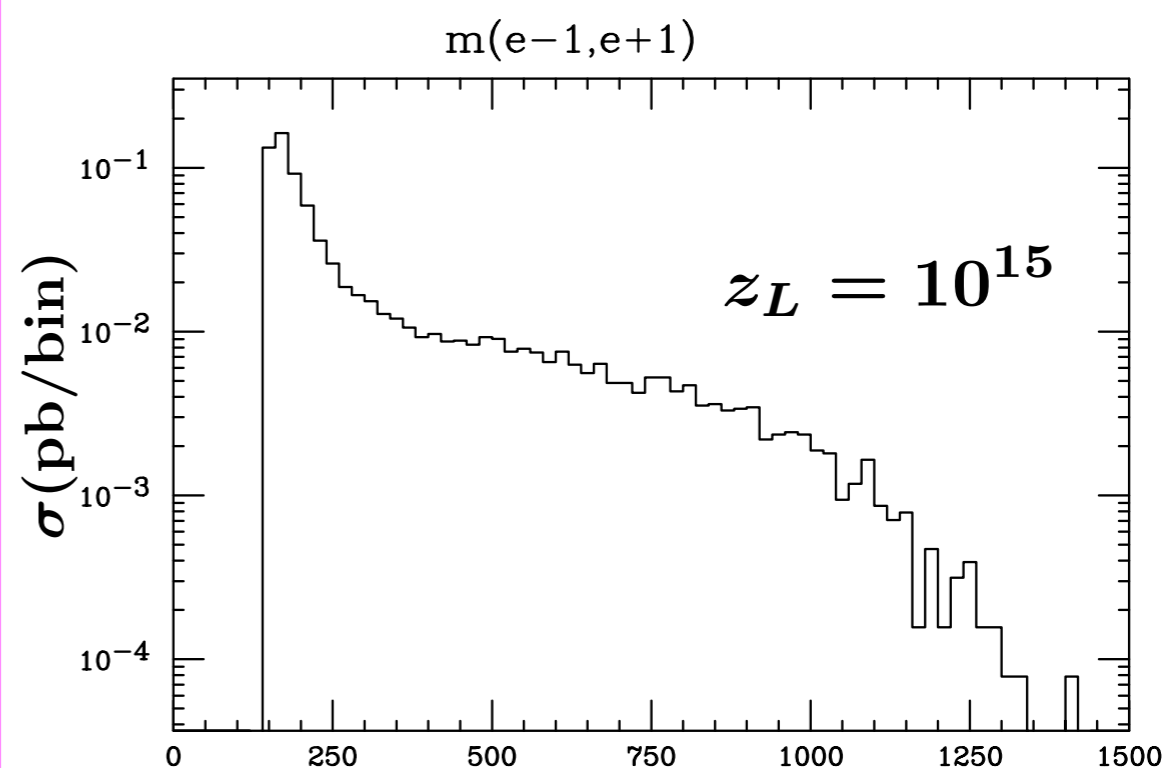
# Z' Search at Tevatron

$$p\bar{p} \rightarrow Z' \rightarrow e^+e^-$$



$$m = 653 \text{ GeV}, \Gamma = 101 \text{ GeV}$$

$$\text{signal } \sigma = 1.8 \text{ pb}$$



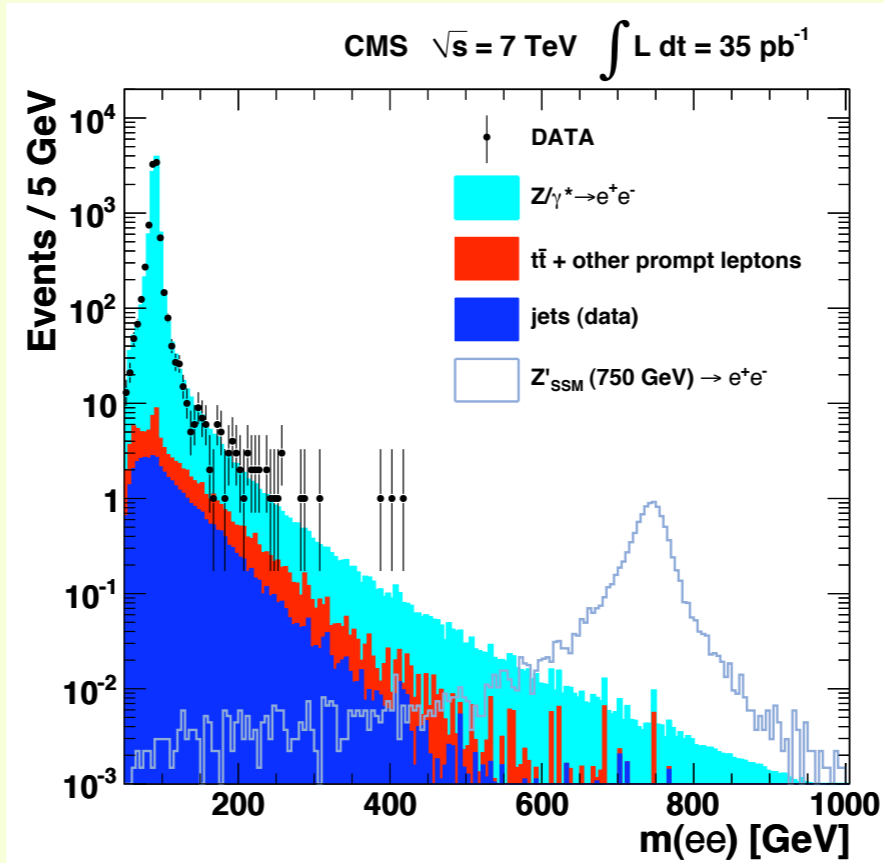
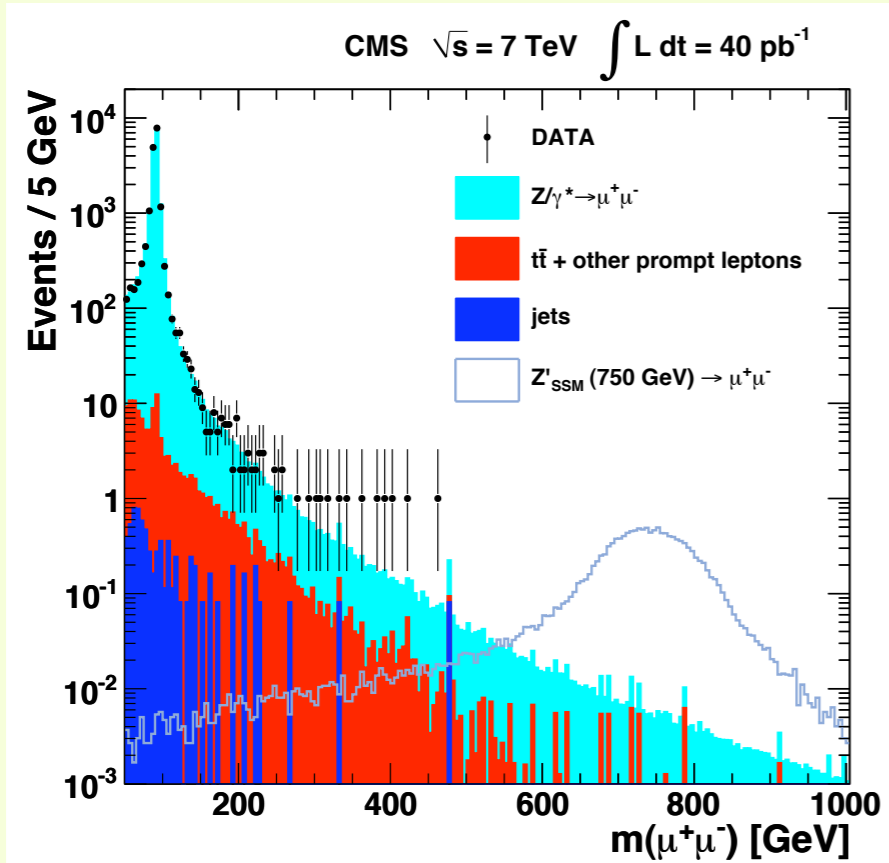
$$m = 1130 \text{ GeV}, \Gamma = 415 \text{ GeV}$$

$$\sigma = 0.06 \text{ pb}$$



$$z_L \geq 10^{15}$$

# Z' Search : CMS 1103.0981

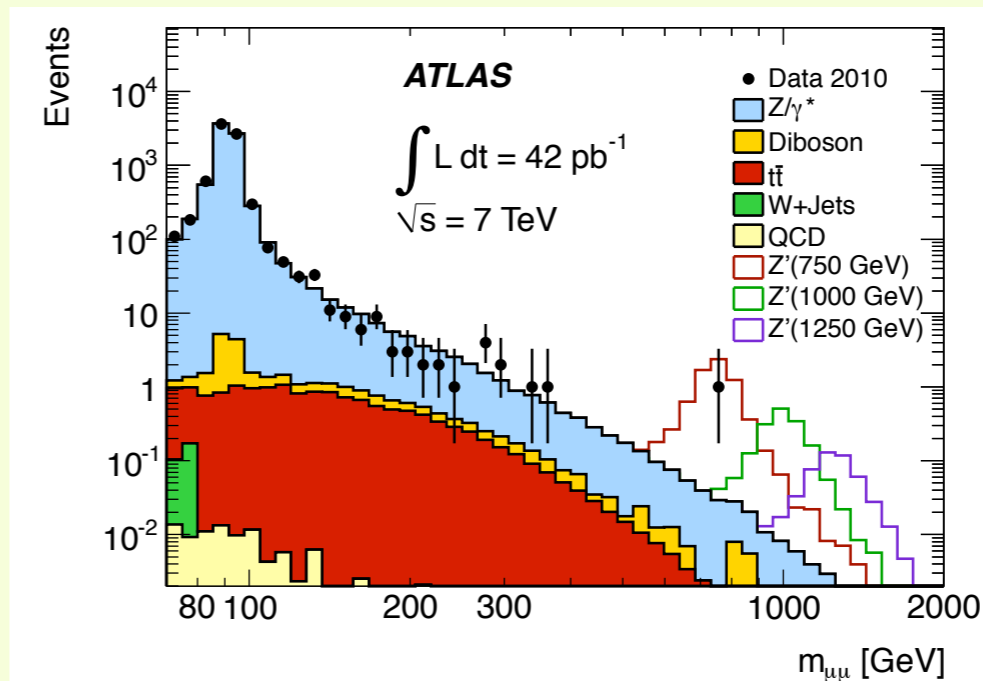
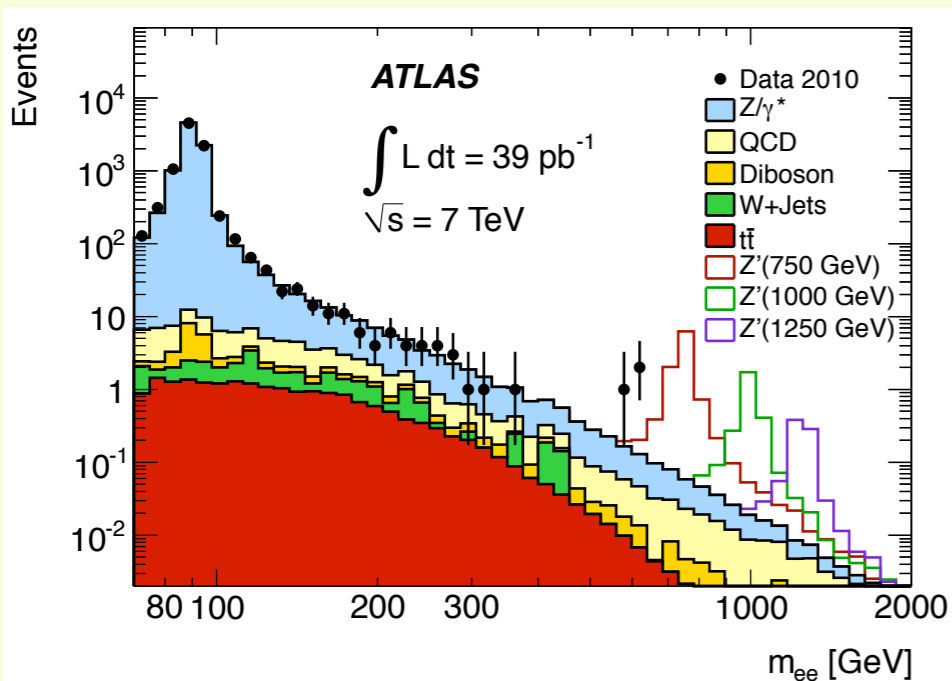


LHC

$$Z'_{\text{SSM}} : \frac{\Gamma}{M} = 0.03$$

$$M > 1140 \text{ GeV}$$

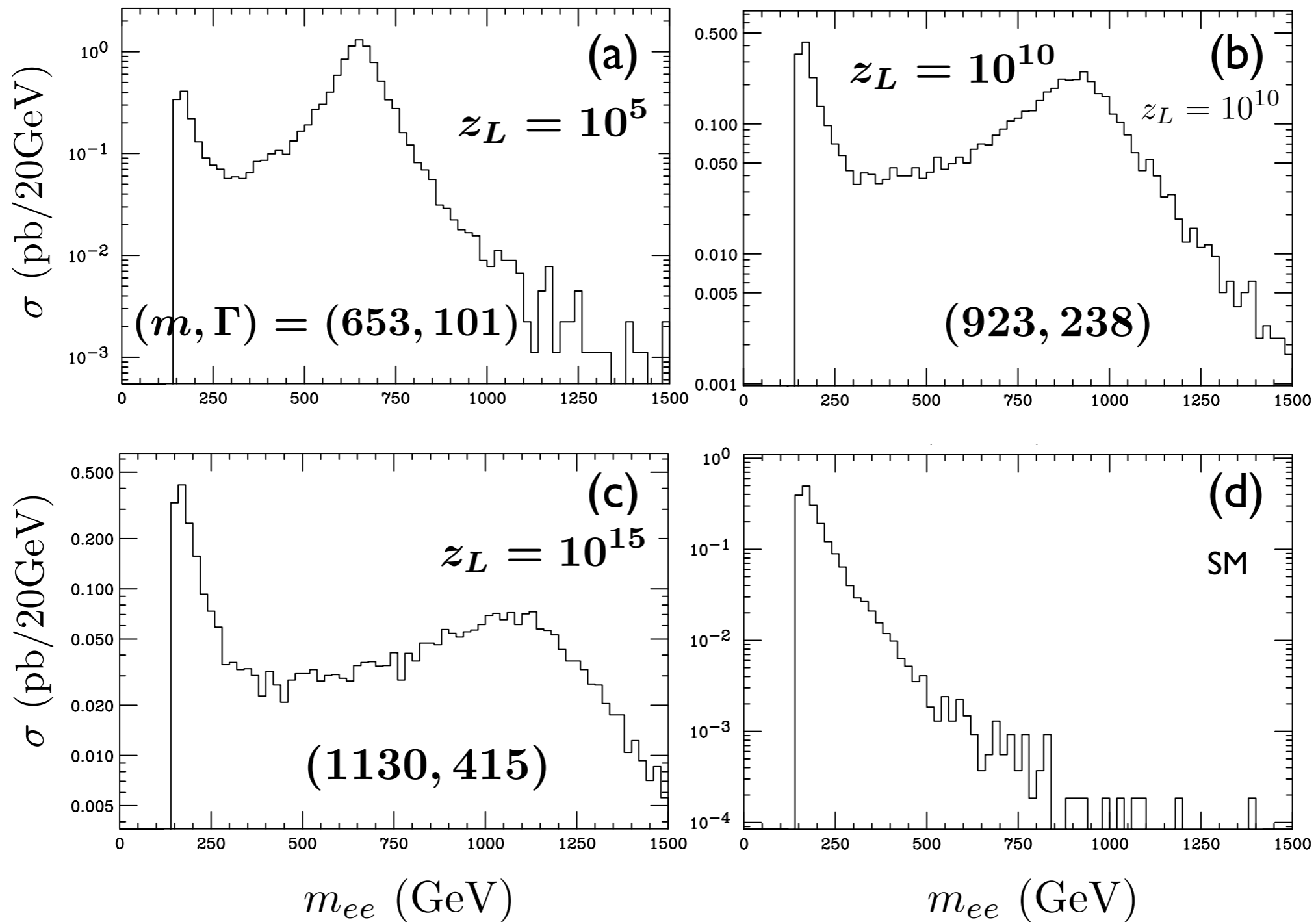
# Z' Search : ATLAS 1103.6218



$$M > 1048 \text{ GeV}$$

# KK Z at LHC (3.5 + 3.5 TeV)

$$q\bar{q} \rightarrow Z^{(1)} \rightarrow e^+e^-$$

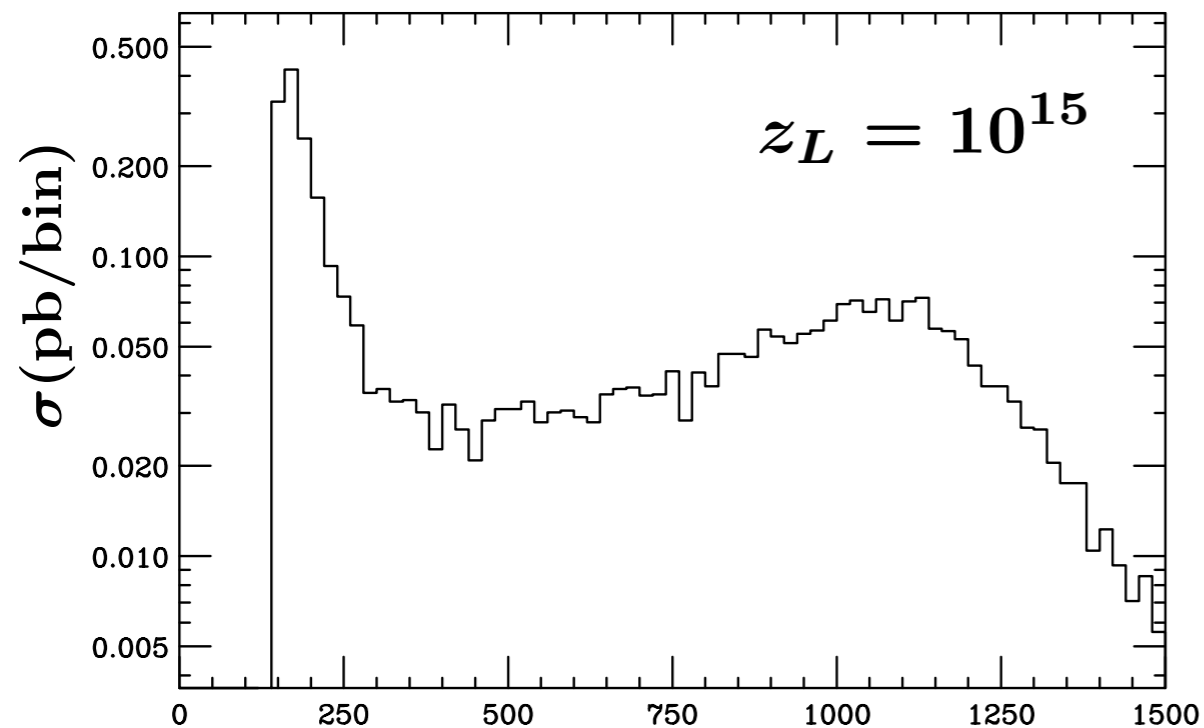




# KK Z at LHC (3.5 + 3.5 TeV)

$$q\bar{q} \rightarrow Z^{(1)} \rightarrow e^+e^-$$

$m(e^-,e^+)$

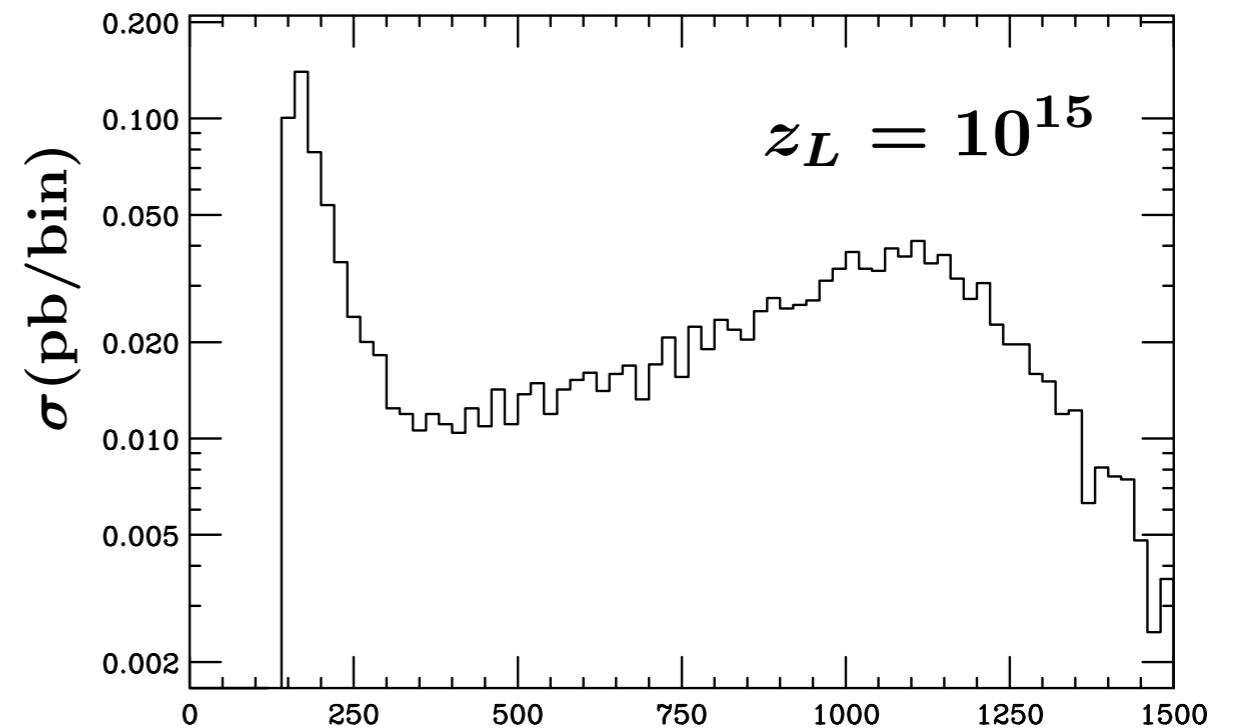


$$m = 1130 \text{ GeV}, \Gamma = 415 \text{ GeV}$$

$$\sigma = 1.9 \text{ pb}$$

$$qg \rightarrow qZ^{(1)} \rightarrow \text{jet} + e^+e^-$$

$m(e^-,e^+)$



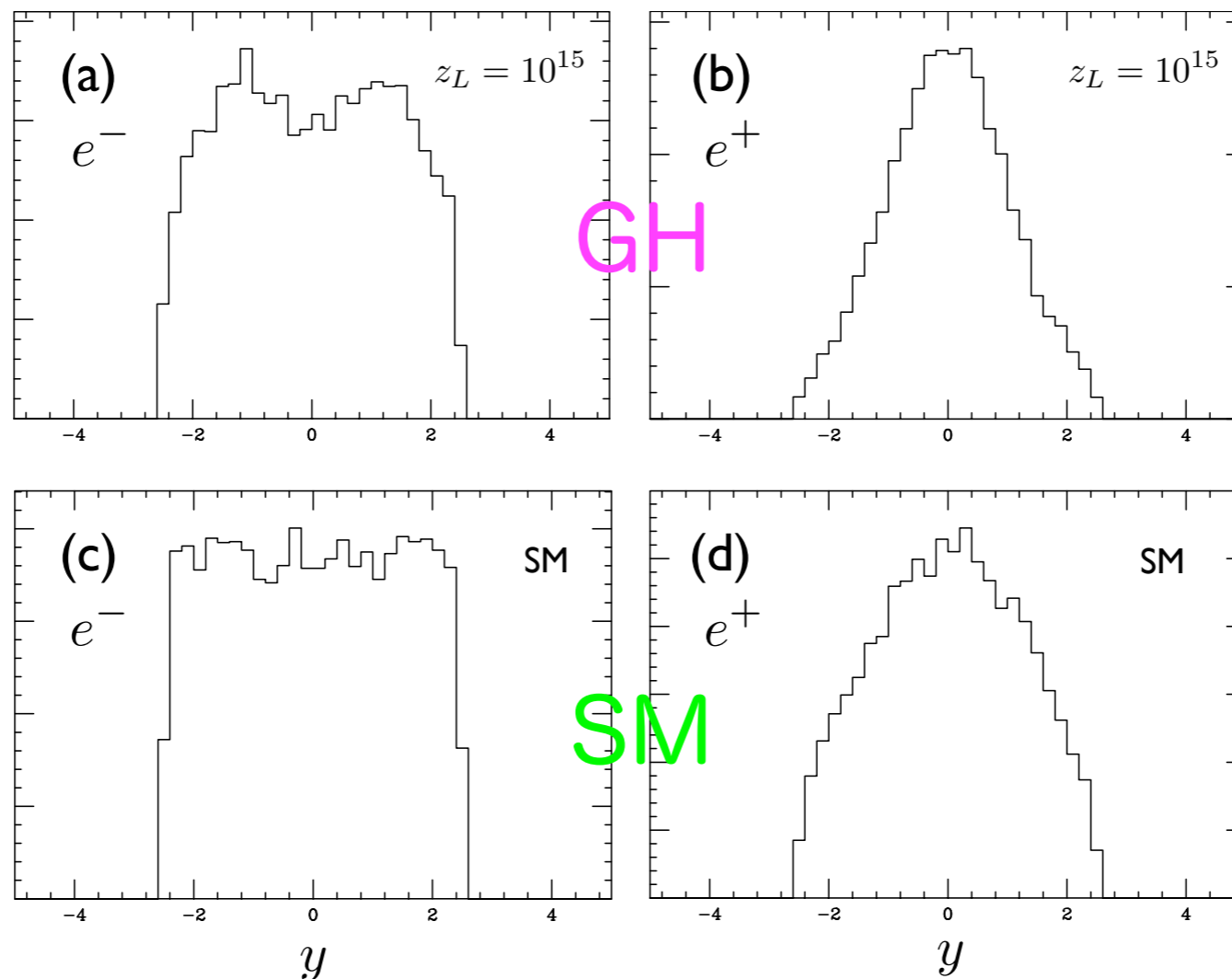
$$m = 1130 \text{ GeV}, \Gamma = 415 \text{ GeV}$$

$$\sigma = 1.0 \text{ pb}$$

**KK  $Z^{(1)}$**

**Large couplings for right-handed quarks and lepton**

**Rapidity distribution**  
 $e^-$  wider than  $e^+$  (in  $pp$  collider)



# KK gluon<sup>(1)</sup>

## Strong couplings for right-handed quarks

Couplings/ $g_s$

$u_R$	6.32
$c_R$	6.04
$t_R$	5.60

$$\Gamma \sim 13 m$$

**Perturbation theory breaks down.**

**No peak.**

**Similar for KK photons.**

# Summary

Gauge-Higgs unification can be tested at LHC.

Higgs naturally becomes stable.

EW precision data  $A_{FB}$ ,  $Z$  decay

$Z'$  search (Tevatron/LHC)  $\Rightarrow z_L \geq 10^{15}$

Find  $Z^{(1)}$  at LHC.

$m \sim 1130 \text{ GeV}$ ,  $\Gamma \sim 415 \text{ GeV}$

Asymmetry in  $e^+e^-$  distribution